



Optimizing the Test Space for Multi-Band Optical Tracking Systems (MBOTS)

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Overview

- Multi-Band Optical Tracking Systems (MBOTS)
- Predictive model for MBOTS performance
- Definition of $p(\text{test success})$



What are MBOTS?

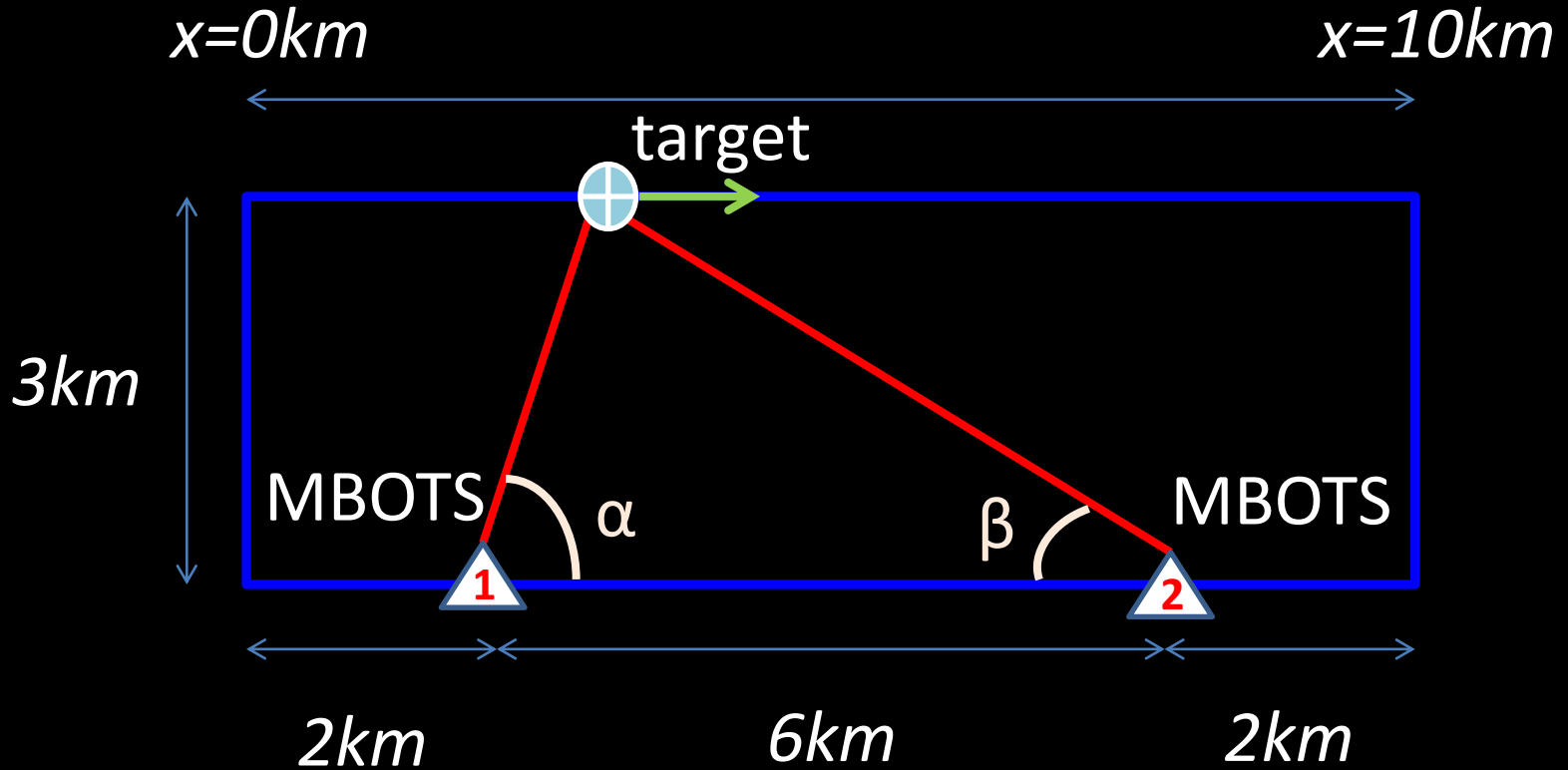
Capabilities

- Track objects
- Record
 - High-speed images
 - Pointing angles
 - Time-space-position info (TSPI)
 - Spectral data

Applications

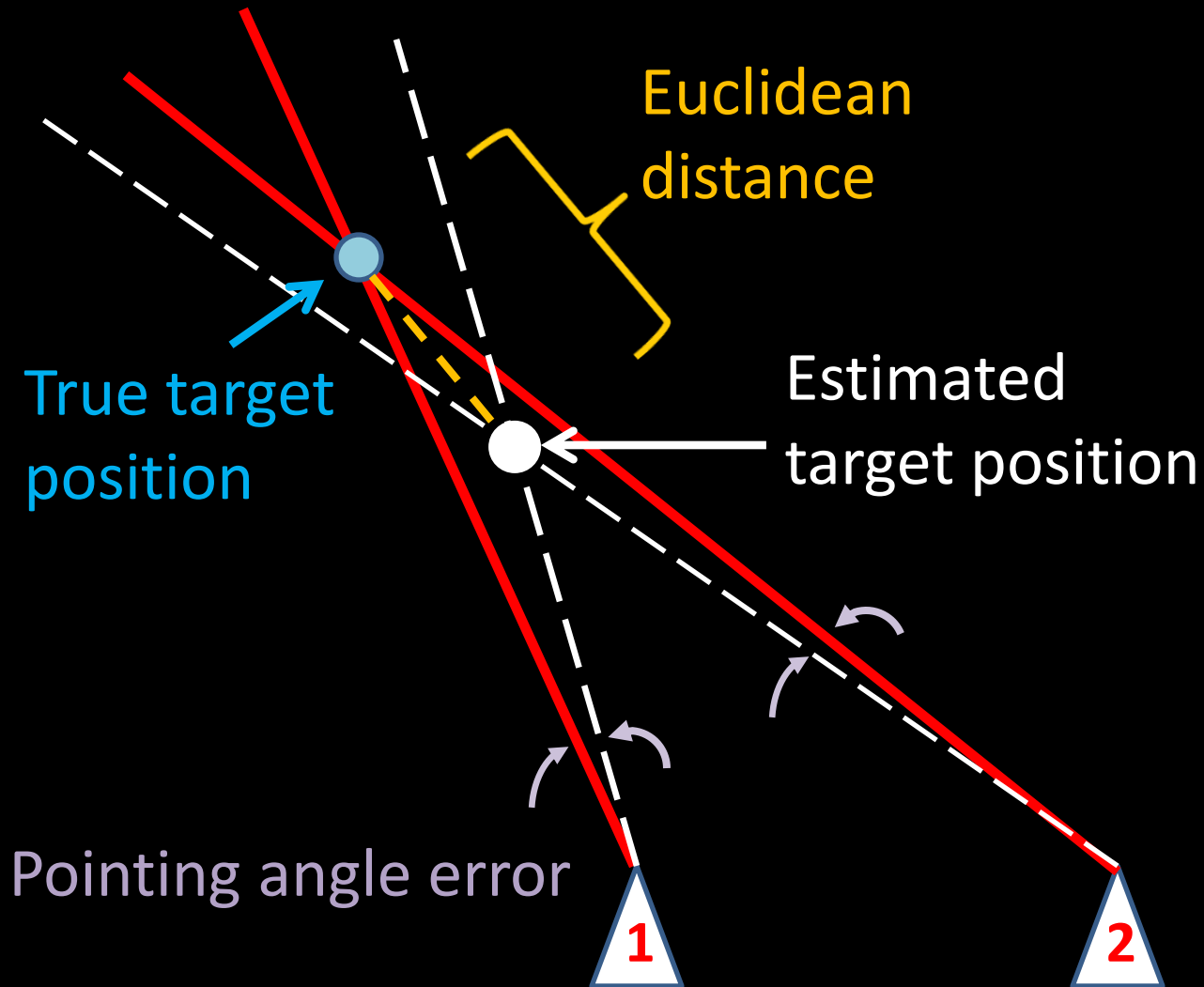
- Laser designation
- Missile testing
- Product Evaluation
- Satellite tracking
- Fire Control
- Surveillance

Test Scenario Geometry



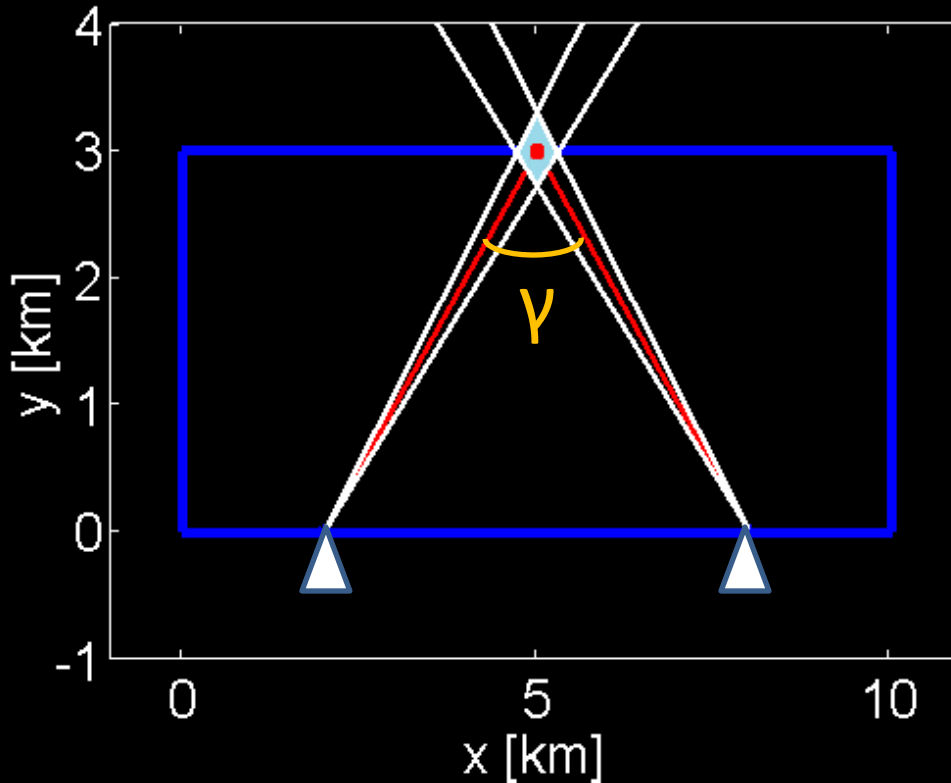
Requirement: Estimate target position to within 1 meter

Error Defined

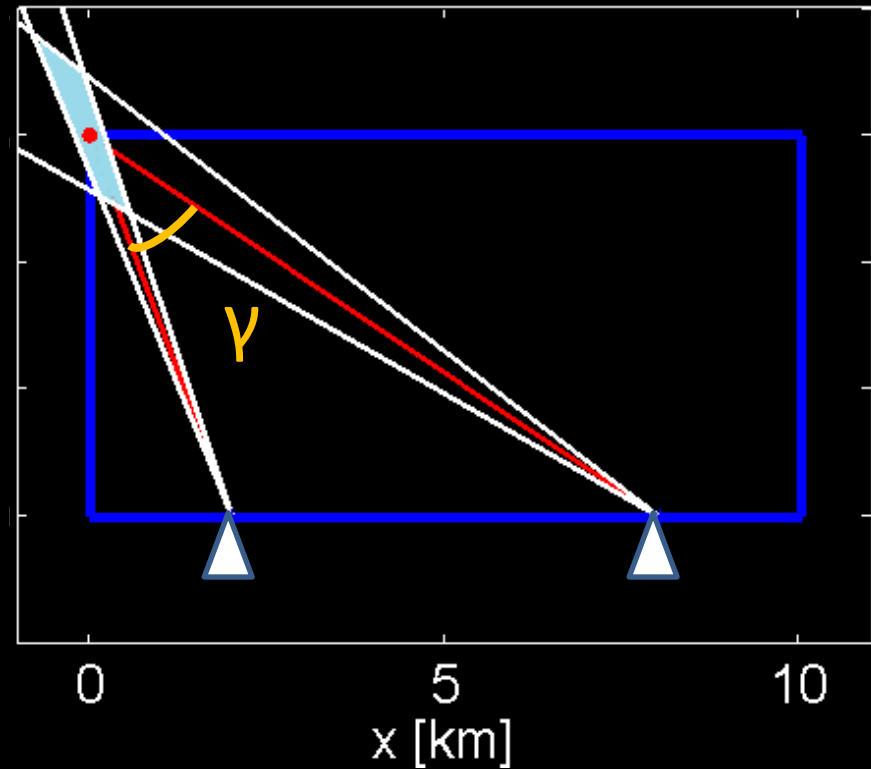


Uncertainty and Viewing Geometry

Favorable



Stressing



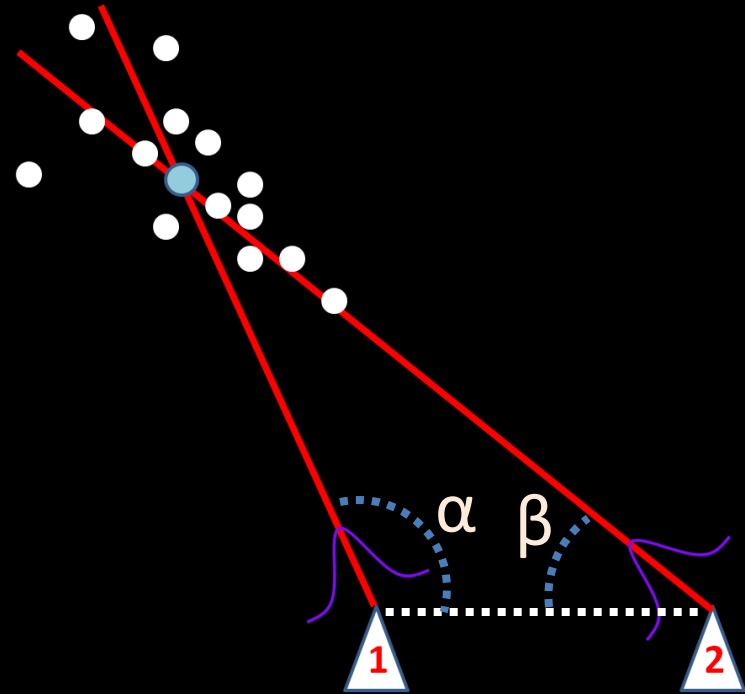
As γ decreases, area of overlap (uncertainty) increases

Monte Carlo Approach

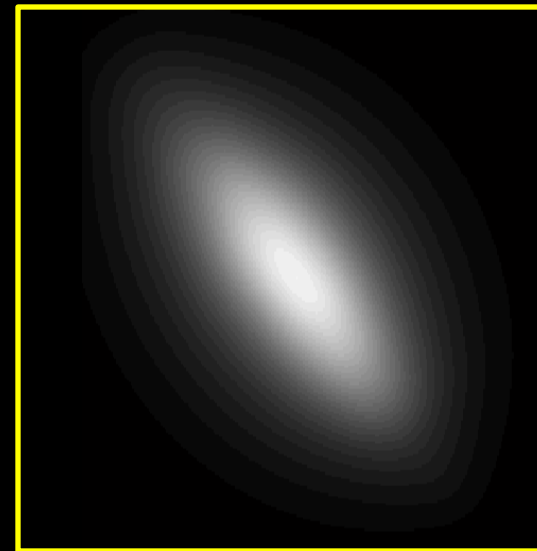
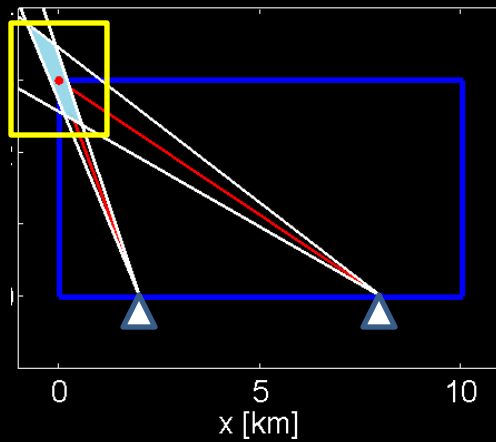
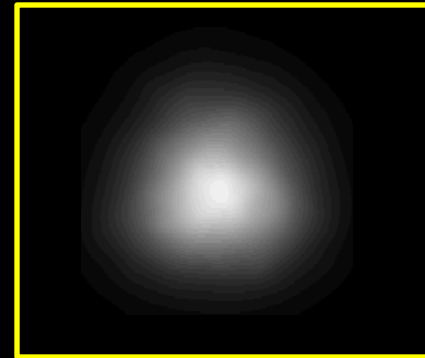
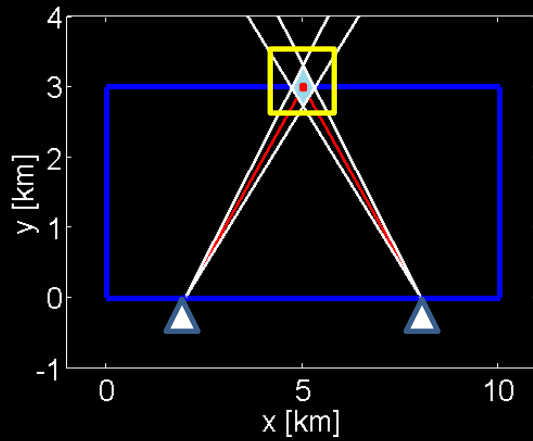
- Draw angles from

$$\alpha_i \sim N(\mu = \alpha, \sigma^2), i = 1, 2, \dots, n$$
$$\beta_i \sim N(\mu = \beta, \sigma^2), i = 1, 2, \dots, n$$

- Determine intersection point between lines-of-sight
- Calculate Euclidean distance between true and estimated target position

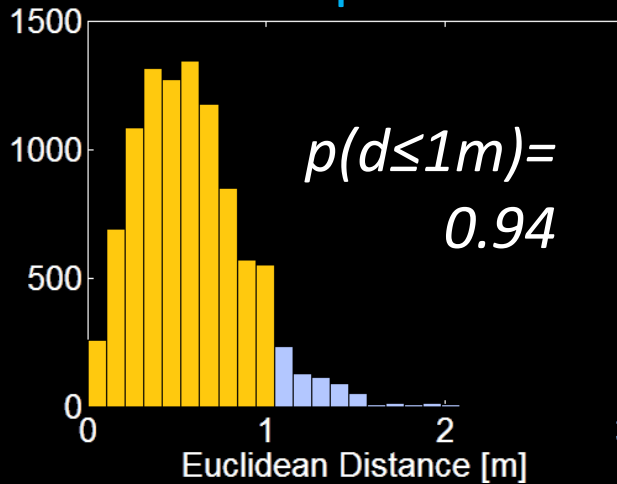


Visualizing Positional Uncertainty

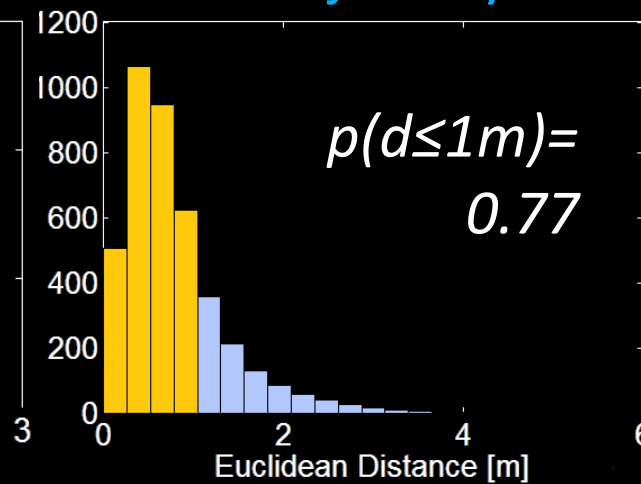


Euclidean Distance Distributions

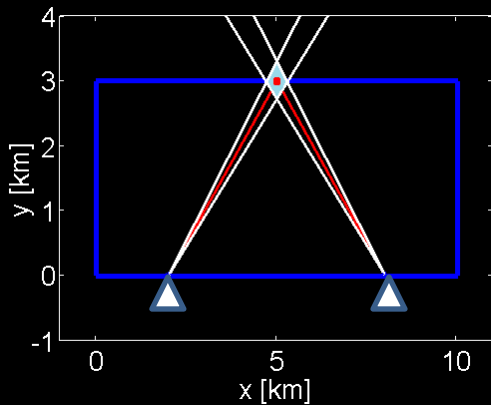
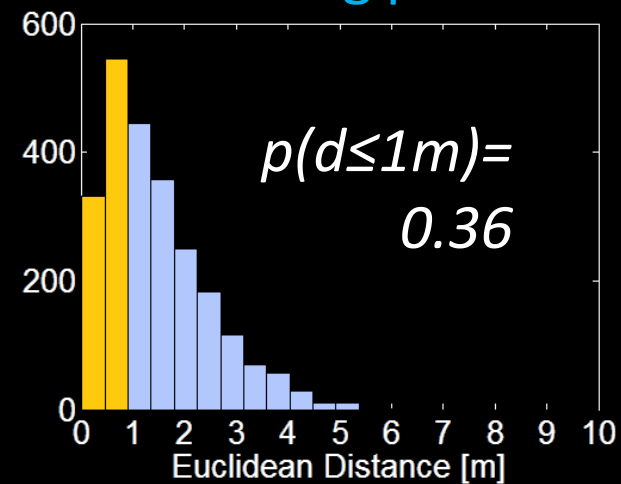
Target at midpoint



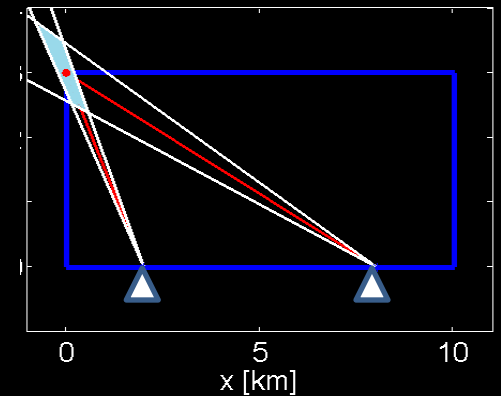
Target across trajectory



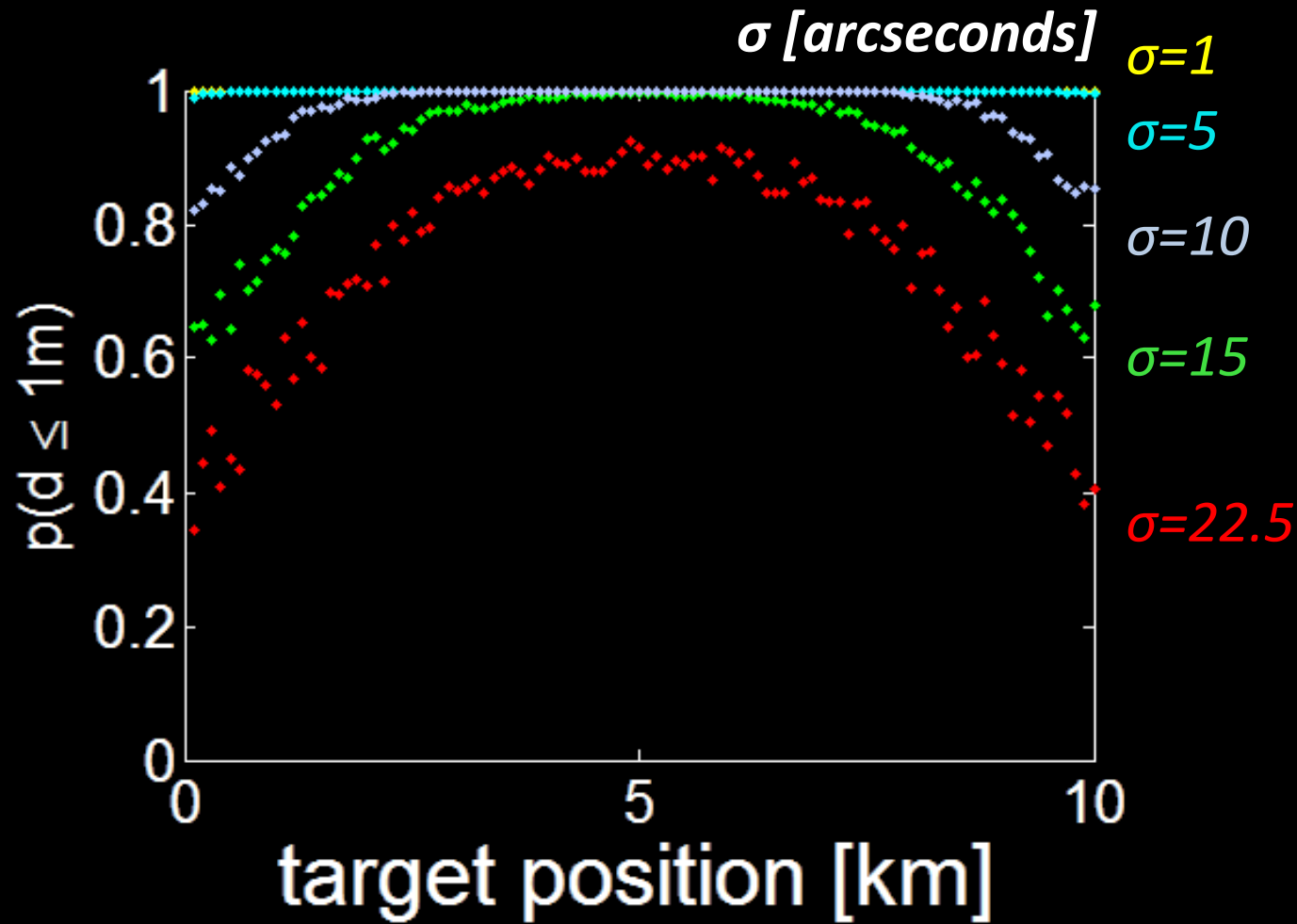
Target at starting point



What do we want to optimize?



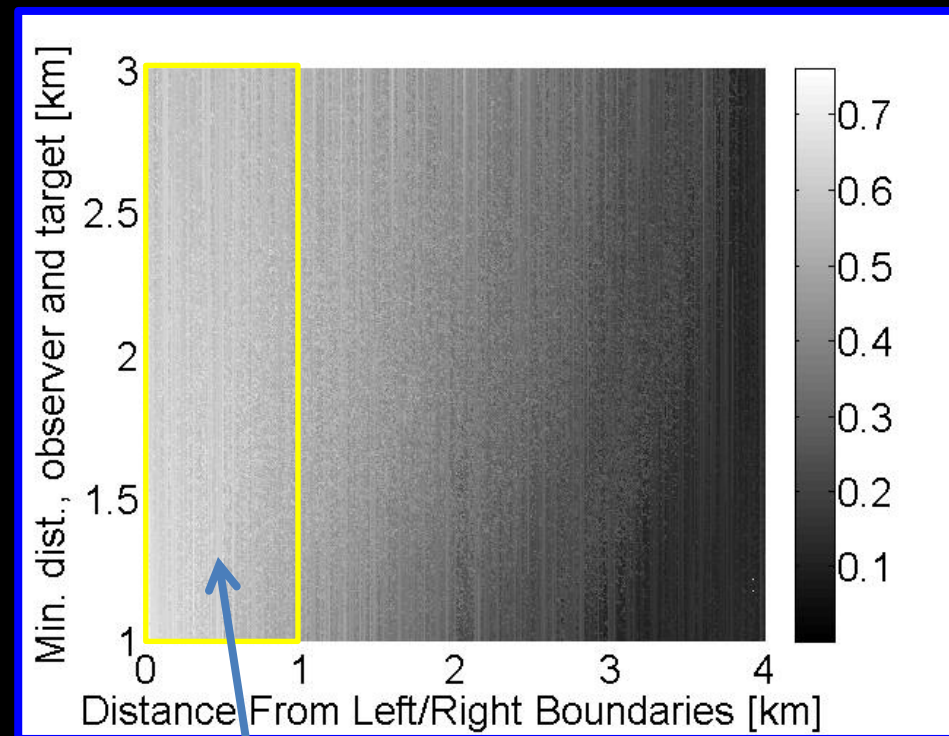
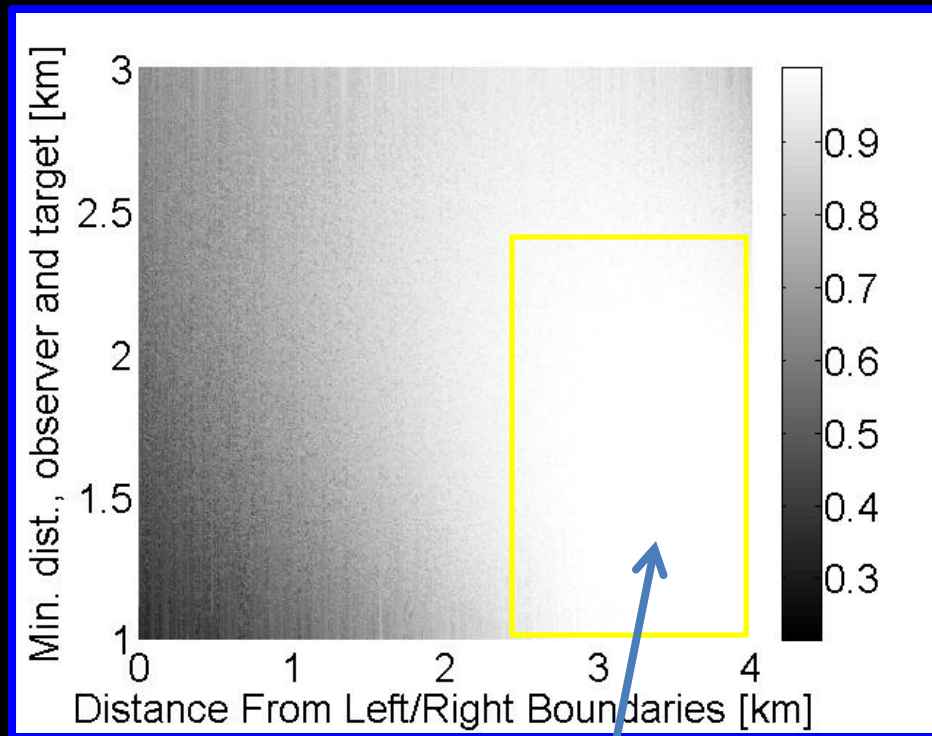
Positional Accuracy vs. Error Budget



Determining Optimal Site Placements

Target at Midpoint of Trajectory

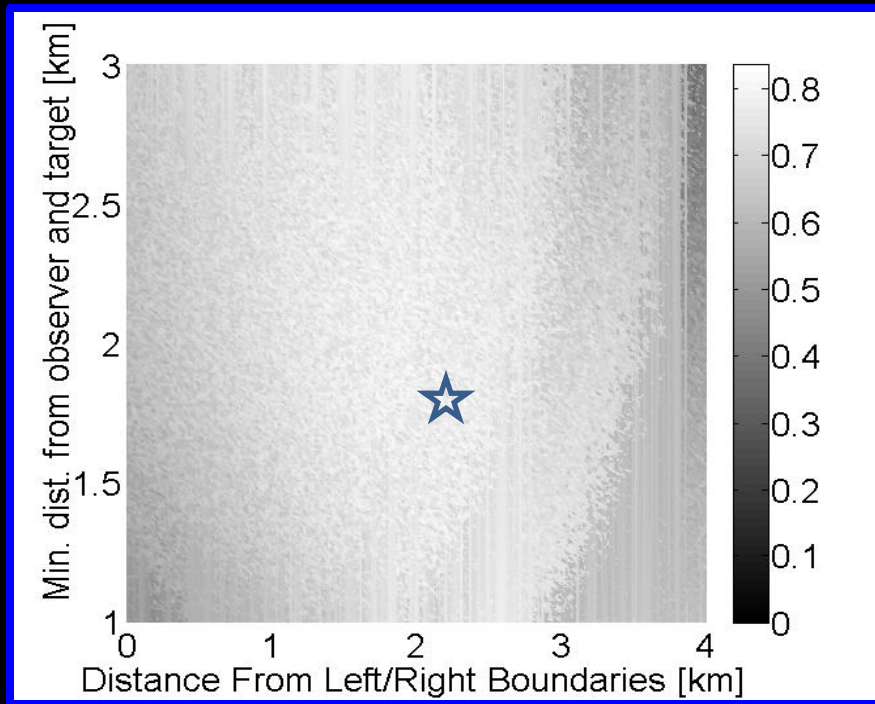
Target at Starting Point of Trajectory



*Wide bounds,
High accuracy*

*Favors the edges,
Reduced accuracy*

Optimal Site Placement Across Trajectory

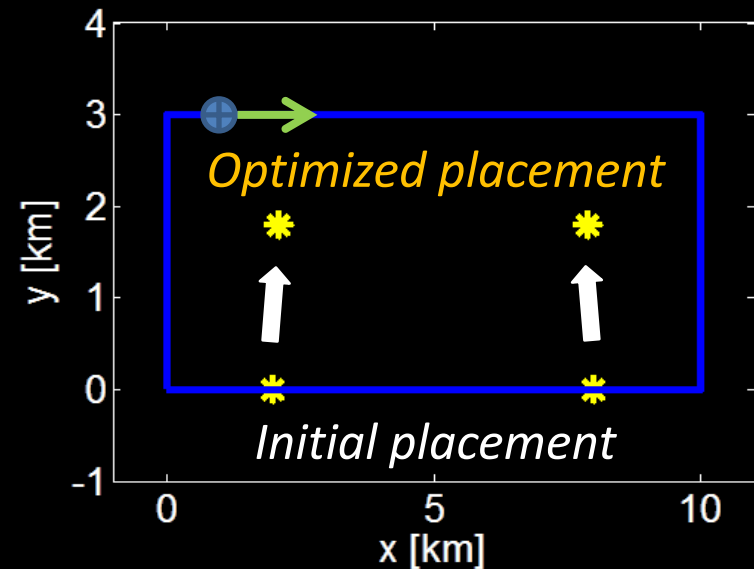


Optimal MBOTS location:

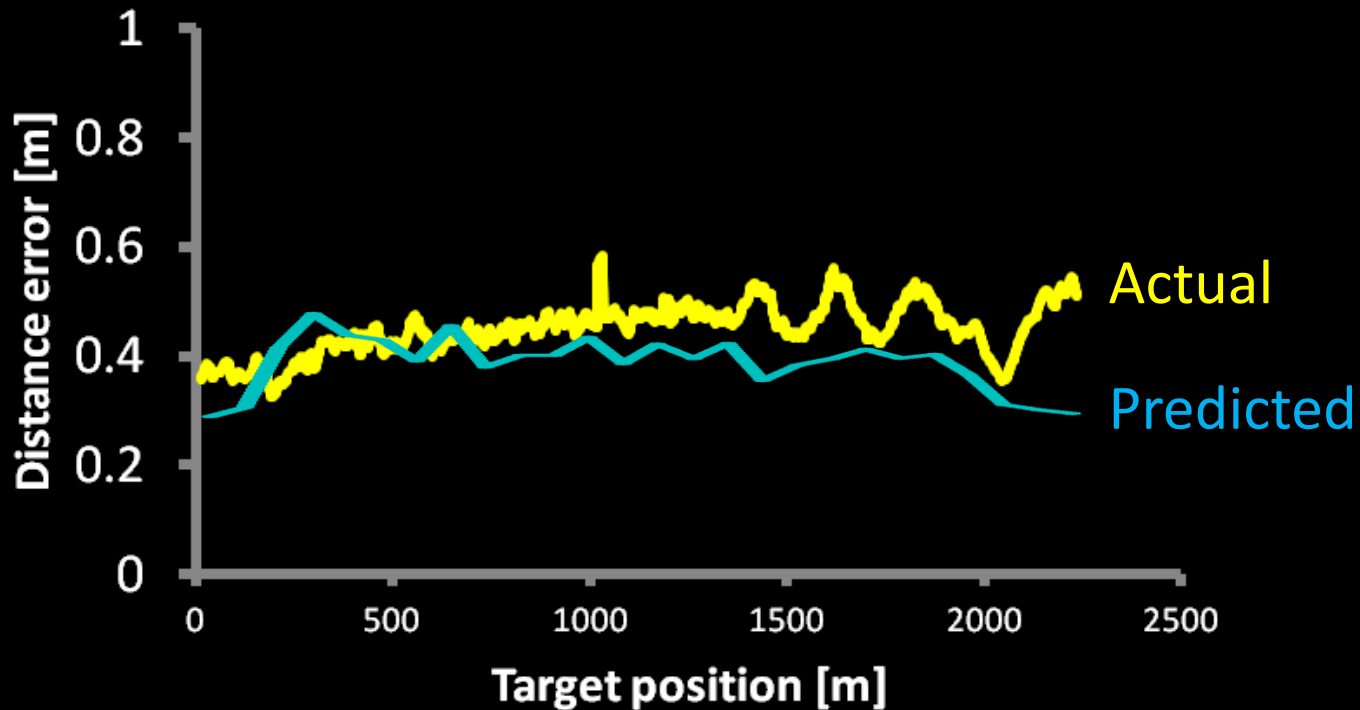
$$(x_1, y_1) = (2.1 \text{ km}, 1.8 \text{ km})$$

and

$$(x_2, y_2) = (7.9 \text{ km}, 1.8 \text{ km})$$



MBOTS Positional Accuracy: Predicted vs. Actual



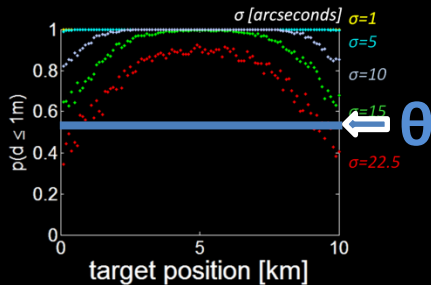
**Data from a site-acceptance test for the Photo-Sonics Mobile Multi-Spectral TSPI System (MMTS), White Sands Missile Range, 2012*

How To Define Success?

Position error $\leq 1\text{m}$



Viewing geometry



$$E \equiv p(\text{Position error} \leq 1\text{m}) \geq \theta$$



*Conditionally
Probabilistic success*

$$p(\text{success} \mid \theta, \sigma) = p[E \mid \theta, \sigma]$$



Way Forward

- MBOTS system accuracy model
 - Future enhancements
 - 6 degrees-of-freedom (DOF) trajectory propagator to support motion dynamics, complex trajectories
 - Modeling of optics, auto-tracker
 - Approach is extensible to multiple MBOTS
- Approach for defining $p(\text{test success})$
 - Result may be used as evidence for T&E resource allocation

Backup



References

1. Downey, G.; Stockum, L. "Electro-Optical Tracking Systems Considerations," Acquisition, Tracking and Pointing III, Vol. 1111, 1989.
2. Joint Range Instrumentation Accuracy Improvement Group, "IRIG Optical Tracking Systems Calibration Catalog," Document 755-99, Secretariat, Range Commanders Council, White Sands Missile Range, New Mexico, February 1999.
3. Das, R.K. "Test and Evaluation of Tactical Missile System Using Electro-Optical Tracking System," ITEA Journal, 30, 2009, 143-148.

Mobile Multi-Spectral TSPI System (MMTS)

Specifications

Nominal Payload	600 lbs.
Maximum Payload	1000+ lbs. with reduced accuracy and performance
Standard Configuration	On-axis optical payload; no man-on-the-mount
Optional Configuration	On-axis optics with off-axis radar
Azimuth Torque	1500 ft lbs
Elevation Torque	2 x 300 ft lbs
Azimuth, Elevation Acceleration	100+ degrees/sec ² with nominal payload
Azimuth, Elevation Velocity	100+ degrees/sec
Weight	6500 lb. trailer-mounted pedestal with single axle
Dimensions	123L x 85W x 80H inches (plus 21" trailer tongue)
Encoder	24-bit absolute position optical encoder with 23-bit quadrature output for velocity

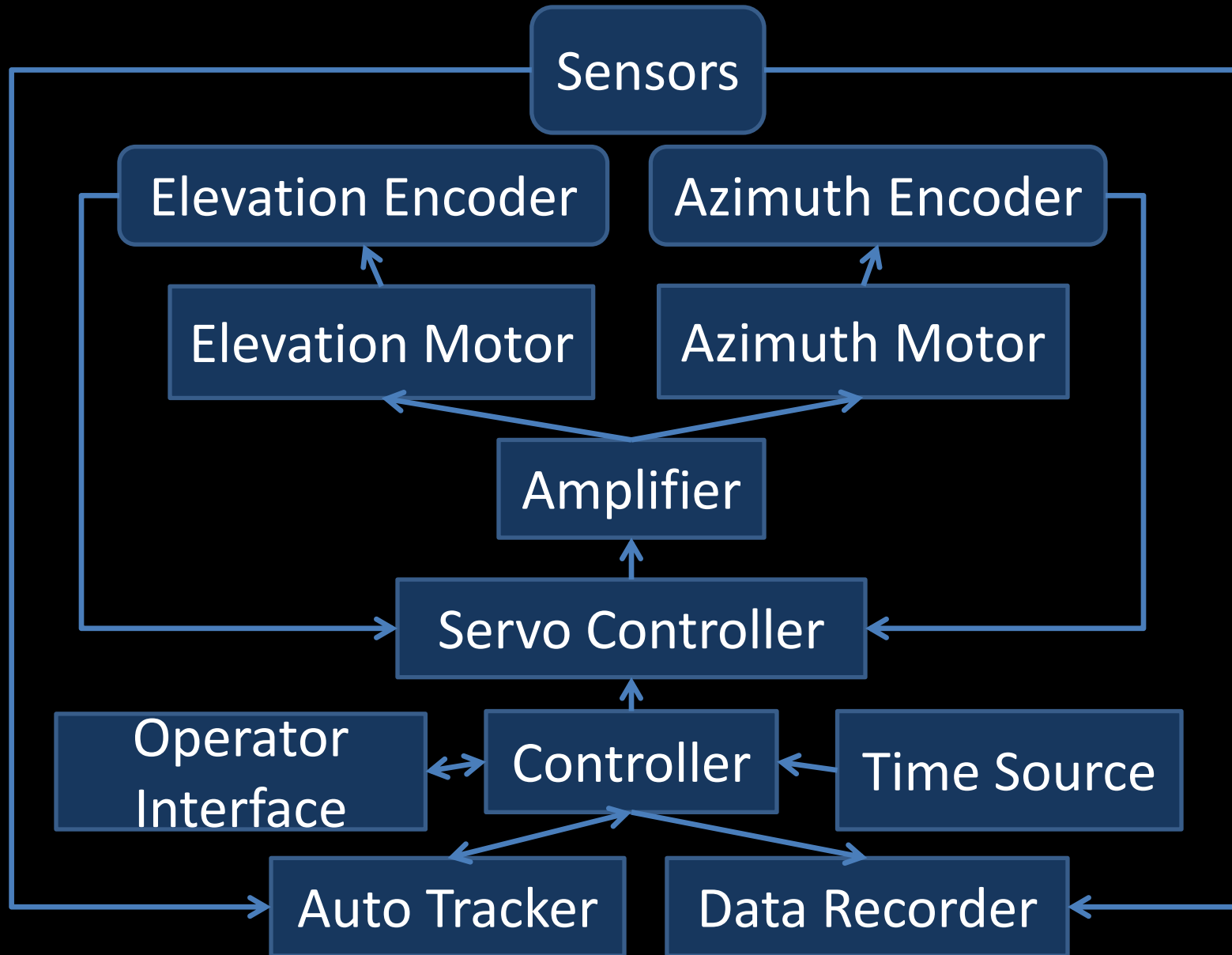
Features:

- Fully Integrated Pedestal and Sensor Control Software
- Real-Time TSPI data output
- Single station solution
- Sensors and System Time-Synchronized to IRIG @ 250 Hz
- Dual gate auto-tracking with Camera Link @ 250 Hz
- Remote Control Console
- Digital Servo Amplifier

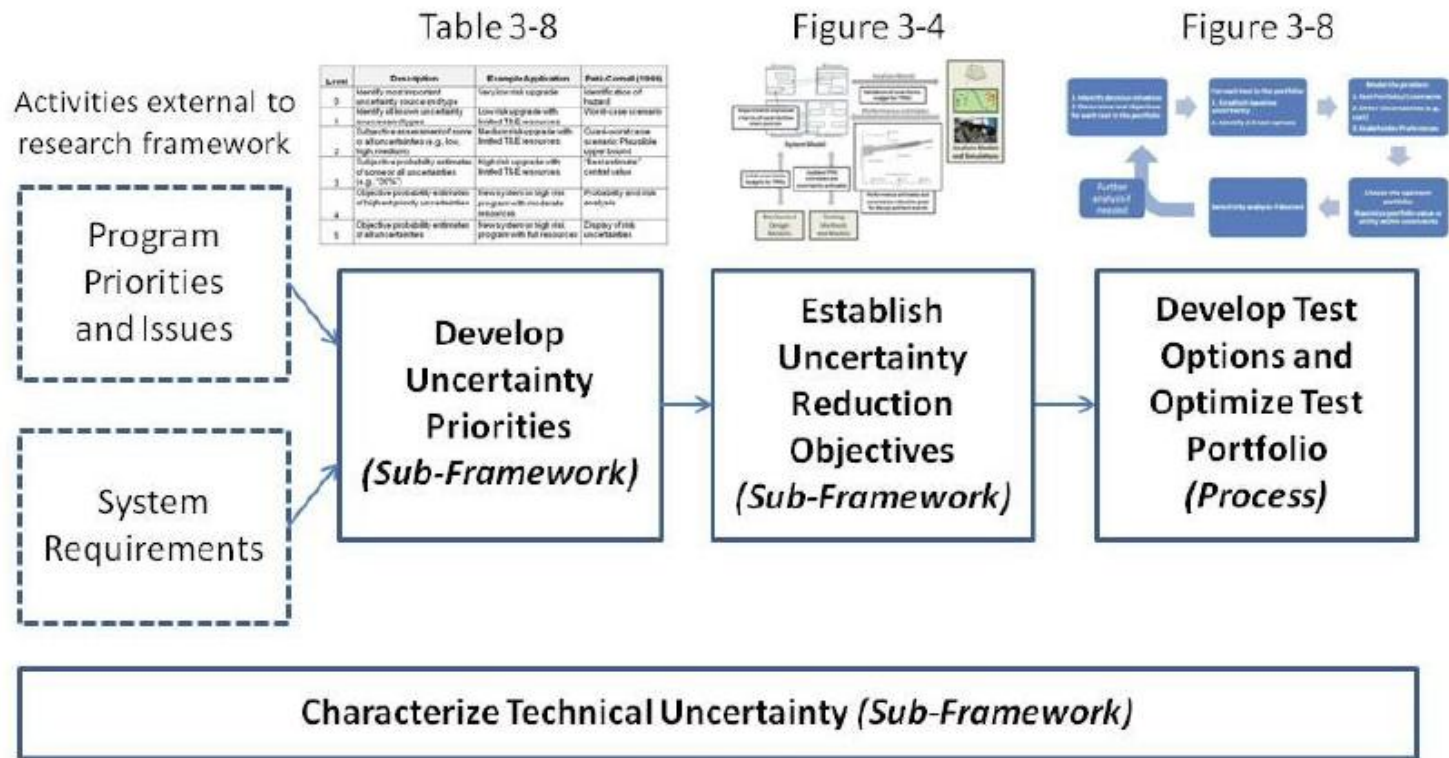
Calibration	Turn & Dump	Star Calibration
No Radar	X	X
Radar on Top		X
Radar on Side	X	X



MBOTS Key Components



Test Value Quantification



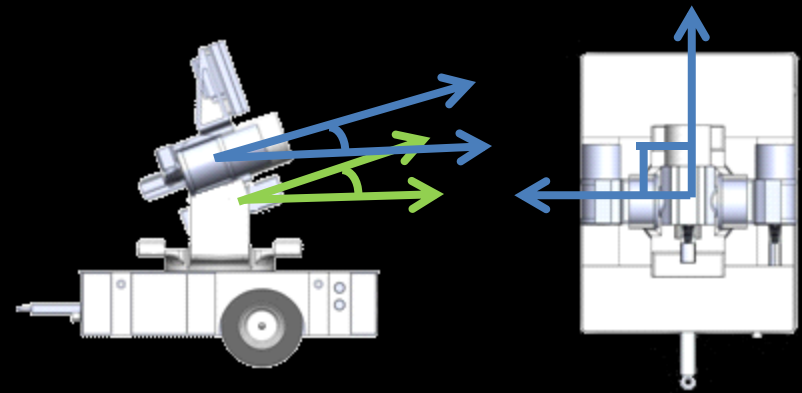
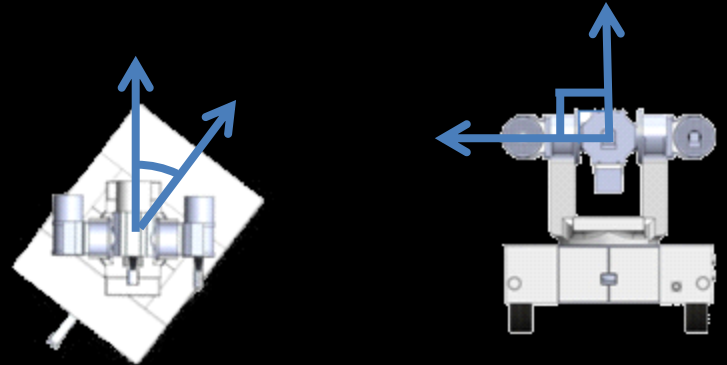
	Unknown Uncertainty	Known Uncertainty (Aleatory)
Essential Elements of Uncertainty	Aleatory	Epistemic
Source of Uncertainty	Measurement input/output, model structure, model selection, prediction error in test uncertainty	
Applicable to Test and Evaluation	Reduce uncertainty	Characterize and Reduce Uncertainty
Type of Data Available	Physical based	None oriented
Characterization of Uncertainty	Stochastic	
Uncertainty Reduction	Model Using and Updating: Using test data to reduce or estimate uncertainty and validate/update model	Model Building: Using data to build model and estimate uncertainty
Uncertainty Characterization (not an objective task)	Probability, Distribution Summary Statistics, Confidence, Prediction or Tolerance Intervals, Credible Interval, Bayesian, Adaptive Information Collection	
Test Value/Uncertainty Estimation	Measure Based on Shannon's Information Entropy	Decision Information Criterion

Table 3-7

*From "Test and Evaluation Resource Allocation Using Uncertainty Reduction as a Measure of Test Value," E. A. Bjorkman, 2012

Systematic Error Sources

- Zero Offset
- Collimation
- Tilt
- Vertical Deflection
- Droop
- Non-orthogonality
- Parallax
- Refraction



Model Assumptions

- 2D model
 - Elevation angle assumed constant, zero degrees
 - Target follows straight path
- CKEM target visible and tracked throughout trajectory
 - 1.5m length, solid-fuel rocket
 - Velocity: 6.5+ Mach